In the paper Priestley-type dualities for partially ordered structures (Annals of Pure and Applied Logic 167 (9), 820-849 (2016), special issue "Fourth Workshop on Formal Topology (4WFTop)") Theorem 2.4 has a missing condition: that for any elements $a, b \in \mathcal{D}$, if $U \cup \{b\} \in \mathcal{I}$ and $a \leq b$ then $U \cup \{a\} \in \mathcal{I}$.

This resulted from the fact that, in calculating the Grothendieck topology J corresponding to the theory $\mathbb{S}_{\mathcal{D}}$, I had forgotten to consider the axiom $(R_a \vdash R_b)$ (for any elements $a, b \in D$ such that $a \leq b$).

This mistake was pointed out by a referee but it was unfortunately reported to me by the Editors of the special issue only after the publication of the paper.

Apologies for any inconvenience caused.